

Laplace

PIK

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Chapter 1

Laplace

1.1 tutorial

- Laplace Manual ↔

----- Tutorial -

4) Turorial

This chapter is still under construction. I will just give some keywords and examples; a more extensive description needs a lot of more work. Please wait for the later releases.

Laplace offers a lot of functions. The easiest way to learn how to use it, is to start with some examples. This should be enough for most applications. For a more detailed view, you should look at the descriptions of the command syntax and internal functions. But I think that those chapters are too detailes for a first introduction.

- *
Analysis
- *
Linear Algebra
- *
Function plotting
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Statistics
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Error distribution
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Programming

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1.2 tutanalysis

- Laplace Manual ----- Analysis -

4.1) Analysis

Define a function

```
> f(x) = x^2
> f(4)
>     => 16
```

Derive a function

The function `derive()` calculated the partial derivation of a given function.

```
> f'(x) = derive( sin(x), x );
> f''(x) = derive( sin(x), x, 2 );
> g(x) = sin(x)
> g'(x) = derive(g)
> h(x,y) = sin(x)*cos(y)
> h'_x(x,y) = derive(h(x,y), x)
> h'_y(x,y) = derive(h(x,y), y)
```

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1.3 tutlinalg

- Laplace Manual ----- Linear Algebra -

4.2) Linear Algebra

Create vectors and matrices

Vectors are always column vectors.

The elements of a matrix row are separated by commas, the rows are separated by semicolons. You can leave out some elements, which are then filled with zeros.

```
> v = [7,9,4]
> M = [4,7,8;6,1,9;7,2,9]
> N = [4;,1;,9]
```

Access elements

```
> v_1 = v[1]
>     => 7
> m_23 = M[2,3]
>     => 9
```

The first element of a vector (row/column of a matrix) has the index one. To fetch a column or row vector of a matrix, use `..` as an index

```
> r = M[2,..]
```

```
> => second row
> c = M[..,1]
> => first column
```

Invert matrix

```
Matrix must be square and det(M) != 0
> invert(M)
```

Matrix determinant

```
Matrix must be square.
> det(M)
```

Gaussian algorithm

The Gaussian algorithm converts the matrix to the form

$$\begin{array}{cccccccc} / & 1 & * & * & * & * & * & \backslash \\ | & 0 & 0 & 1 & * & * & * & | \\ | & 0 & 0 & 0 & 1 & * & * & | \\ | & 0 & 0 & 0 & 0 & 0 & 1 & | \\ \backslash & 0 & 0 & 0 & 0 & 0 & 0 & / \end{array}$$

```
> gsolve(M)
```

Matrix rank

```
Apply the Gaussian algorithm and count non-zero rows.
> rank(M)
```

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1.4 tutplot

- Laplace Manual ----- Function plotting -

4.3) Function plotting

Simple plot of an expression:

```
> plot(x^2, x)
> plot(sin(y)^2, y)
> f(x) = x^3 - x^2 + 4
> plot(f(x), x=0..10)
```

Simple animated plot of an expression:

```
> animate(sin(y*sinh(x))^2, x, y)
```

Several graphs in one window:

```
> p = plot_new()
> plot_addfunc(p, x^2, x)
> plot_addfunc(p, sin(y), y)
> plot_open(p)
```

```

Several graphs in one window (animated):
> p = plot_newanim()
> plot_addfunc(p, x^(2+t), x, t)
> plot_addfunc(p, sin(y)*exp(z*y), y, z)
> plot_open(p)

```

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1.5 tutstats

- Laplace Manual ----- Statistics -

4.4) Statistics

Don't forget to load the standard.lh library

```
> include("Init.lh")
```

In most cases it is useful to enable floatpoint calculations:

```
> $usefloat = TRUE
```

Create a array of numbers:

```
> A = array(75.8, 74.6, 76.2, 75.5, 75.9, 78.0, 79.2, 74.7, 75.5, 75.3)
```

Calculate average value of this array

```
> average(A)
> => 76.07
```

Calculate standard variation

```
> sigma(A)
> => 1.449943
```

Relative error of this array is

```
> error(A)
> => 0.458512
```

Your final average value is 76.07 ± 0.46

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1.6 tuterrdist

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4.5) Error distribution

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1.7 tutprog

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4.6) Programming

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